

APPLYING KINEMATIC EQNS TO BODIES UNDER FREE-FALL CONDITIONS

#1



$$\vec{v}_1 = 0 \text{ m/s}$$

$$\vec{a} = 9.8 \text{ m/s}^2$$

$$\Delta \vec{d} = 12 \text{ m}$$



(a) $\Delta t = ?$

$$\Delta \vec{d} = \vec{v}_1 \Delta t + \frac{1}{2} \vec{a} \Delta t^2$$

$$12 = 4.9 \Delta t^2$$

$$\Delta t = 1.56 \text{ s}$$

(b) $\vec{v}_2 = ?$

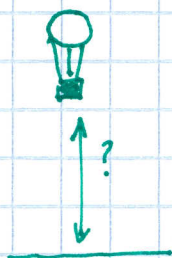
$$\vec{v}_2^2 = \vec{v}_1^2 + 2 \vec{a} \Delta \vec{d}$$

$$= 2(9.8)(12)$$

$$\vec{v}_2 = \sqrt{235.2}$$

$$= 15.34 \text{ m/s}$$

#2



$$\vec{v}_1 = 0 \text{ m/s}$$

$$\vec{v}_2 = 73 \text{ m/s}$$

$$\vec{a} = 9.8 \text{ m/s}^2$$



(a) $\Delta \vec{d} = ?$

$$\vec{v}_2^2 = \vec{v}_1^2 + 2 \vec{a} \Delta \vec{d}$$

$$73^2 = 19.6 \Delta \vec{d}$$

$$\Delta \vec{d} = 271.9 \text{ m}$$

(b) $\Delta t = ?$

$$\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$$

$$73 = 9.8 \Delta t$$

$$\Delta t = 7.45 \text{ s}$$

#3

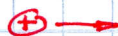


$$\vec{v}_1 = 0 \text{ m/s}$$

$$\vec{a} = 2.4 \text{ m/s}^2$$

$$\vec{v}_2 = 61 \text{ m/s}$$

$$\Delta \vec{d} = ?$$

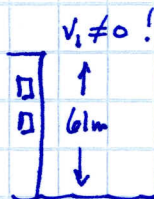


$$\vec{v}_2^2 = \vec{v}_1^2 + 2 \vec{a} \Delta \vec{d}$$

$$61^2 = 4.8 \Delta \vec{d}$$

$$\Delta \vec{d} = 775 \text{ m}$$

#4



$v_i \neq 0$

$$\vec{v}_1 = ?$$

$$\vec{a} = 9.8 \text{ m/s}^2$$

$$\Delta \vec{d} = 61 \text{ m}$$

$$\Delta t = 3.1 \text{ s}$$



$$\Delta \vec{d} = \vec{v}_1 \Delta t + \frac{1}{2} \vec{a} \Delta t^2$$

$$61 = 3.1 \vec{v} + 4.9(3.1)^2$$

$$13.91 = 3.1 \vec{v}$$

$$\vec{v} = 4.49 \text{ m/s}$$

#5



(c)

$$\vec{v}_1 = 33 \text{ m/s}$$

$$\vec{a} = -9.8 \text{ m/s}^2$$

$$\vec{v}_2 = 0 \text{ m/s}$$

$$\Delta \vec{d} = ?$$



$$\vec{v}_2^2 = \vec{v}_1^2 + 2 \vec{a} \Delta \vec{d}$$

$$0 = 33^2 + 2(-9.8) \Delta \vec{d}$$

$$\Delta \vec{d} = 55.6 \text{ m}$$

(b) time to go up = time to go down

$$\vec{v}_1 = 33 \text{ m/s}$$

$$\vec{a} = -9.8 \text{ m/s}^2$$

$$\vec{v}_2 = 0 \text{ m/s}$$

$$\Delta t = ?$$

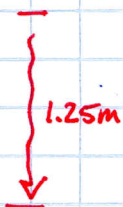
$$\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$$

$$0 = 33 - 9.8 \Delta t$$

$$\Delta t = 3.37 \text{ s (up)}$$

$$\therefore \Delta t = 6.74 \text{ s}$$

#6



$$v_i = 0 \text{ m/s}$$

$$\vec{a} = 1.62 \text{ m/s}^2$$

$$\Delta d = 1.25 \text{ m}$$

$$\Delta t = ?$$

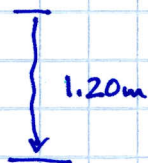
$$\oplus \quad (a) \quad \Delta \vec{d} = \vec{v}_i \Delta t + \frac{1}{2} \vec{a} \Delta t^2$$

$$1.25 = \frac{1}{2} (1.62) \Delta t^2$$

$$\Delta t = 1.24 \text{ s}$$

(b) It would take the hammer the same time since its acceleration would be the same.

#7



$$v_i = 0 \text{ m/s}$$

$$\vec{a} = 9.8 \text{ m/s}^2$$

$$\Delta d = 1.20 \text{ m}$$

$$\Delta t = ?$$

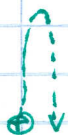
$$\vec{v}_2 = ?$$

$$\vec{v}_2^2 = \vec{v}_i^2 + 2 \vec{a} \Delta d$$

$$= 0 + 2(9.8)(1.20)$$

$$\vec{v}_2 = 4.85 \text{ m/s}$$

#8



$$\vec{v}_i = ? = v \quad \oplus$$

$$\vec{a} = -9.8 \text{ m/s}^2$$

$$\Delta t = 2.8 \text{ s}$$

$$\vec{v}_2 = ? = -v$$

$$\vec{v}_2 = \vec{v}_i + \vec{a} \Delta t$$

$$-v = v - 9.8(2.8)$$

$$-2v = -27.44$$

$$v = 13.72 \text{ m/s}$$

OR

Consider only the motion up.
In this case $\Delta t = \frac{1}{2}(2.8)$
 $= 1.4 \text{ s}$

and $v_2 = 0 \text{ m/s}$.

$$\vec{v}_2 = \vec{v}_i + \vec{a} \Delta t$$

$$0 = \vec{v}_i - 9.8(1.4)$$

$$\vec{v}_i = 13.72 \text{ m/s}$$